

## **MATHEMATICAL SIMULATION IN CENTER OF GRAVITY POSITION FOR A BIPED ROBOT**

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**Abstract:** This paper aims to present special issues concerning the analysis of mobile robots with kinematic motion effects on the stability study. In the analysis, the authors used inverse kinematics, which enables rapid modelling and identifying solutions as regards the stability of bipedal robots. The symbolic solution for kinematics equations of biped robots is of great importance for the efficient controllability of these robots. The following article focuses on the biped robot center of gravity simulation and control handle with the aid of mathematical modeling methods (in MATLAB)

### **1. INTRODUCTION**

For a biped robot the sole position and orientation is known, defined within the domain of exterior coordinates, if a  $\vec{q}$  vector is given with joint coordinates. In the case of a robot with n freedom degree, the vector of joint variables is [2], [6] the following:

$$\vec{q} = [q_1, q_2, \dots, q_{n-1}, q_n]^T. \quad (1.1)$$

And the vector of unknown exterior coordinates is the following:

$$x_q = [x_{q1}, x_{q2}, \dots, x_{qn-1}, x_{qn}]^T. \quad (1.2)$$

The equation below is the only solution for the so called direct kinematics problem.

$$x_q = f(\vec{q}). \quad (1.3)$$

If we know sum of the joint's setup and from this we define the coordinate system's position, according to the sole's centre point, as well as its orientation, thus we solved the direct kinematics problem. Inverse kinematics problem means that if the sole's expected position and orientation (within the exterior coordinates) is known, and then with which joint setups can we obtain this. In other words we can say that we are looking for only solution.

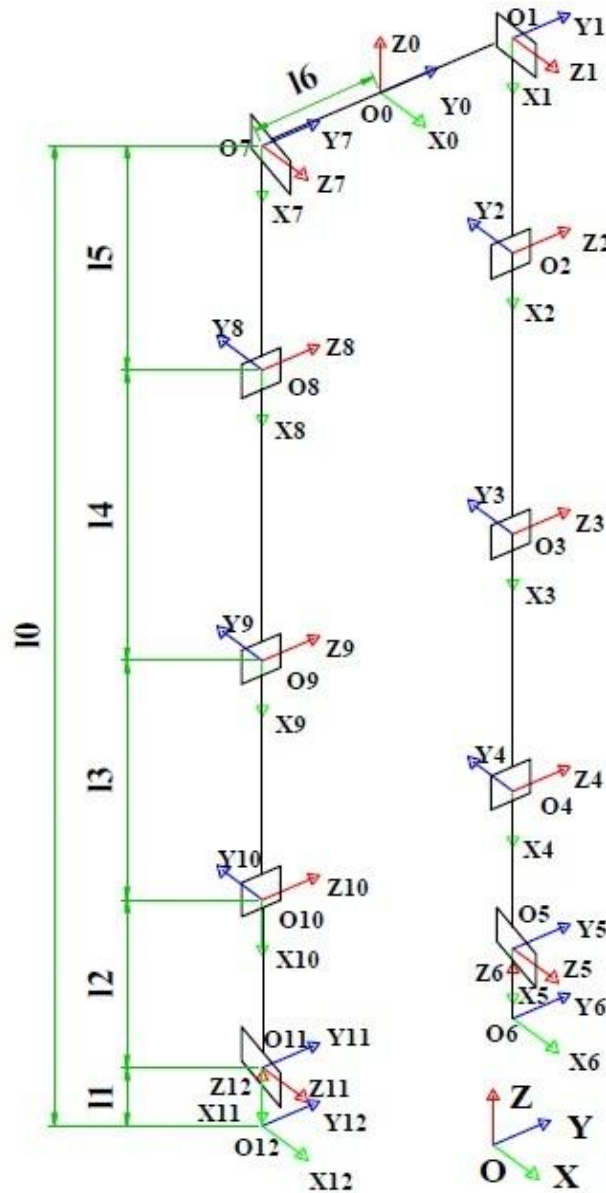
$$\vec{q} = f^{-1}(x_q). \quad (1.4)$$

This task is more complex than the direct kinematics problem, since it is not linear, we have to solve equations containing trigonometric functions. The symbolic solution for kinematics equations of biped robots is of great importance for the efficient controllability of these robots.

The symbolic form of the kinematics equations describes explicitly in trigonometric form the biped robots' sole's position and orientation according to the joint coordinates. In this case, the equation in the range of real numbers can be solved with the minimal possible operations.

## 2. Kinematic modeling

Direct kinematics problem is to define all relationships that end-effector position (foot of biped robot) based on joint coordinates practically [2], [4], [5], it ensures internal coordinates conversion (joint) Coordinate external (operational).



*Figure 1. Kinematic model*

Biped robot kinematics equations are (Figure 1.):

$$T_{06} = \begin{bmatrix} -c_{q_{234}} & \sin(q_6) \cdot s_{q_{234}} & \cos(q_6) \cdot c_{(q_{234})} \\ -\sin(q_1) \cdot s_{q_{234}} & \cos(q_1) \cdot \cos(q_6) + \sin(q_1) \cdot \sin(q_6) \cdot c_{q_{234}} & \cos(q_1) \cdot \cos(q_6) + \sin(q_1) \cdot \sin(q_6) \cdot c_{q_{234}} \\ \cos(q_1) \cdot s_{q_{234}} & -\sin(q_1) \cdot \cos(q_6) + \cos(q_1) \cdot \sin(q_6) \cdot c_{q_{234}} & -\sin(q_1) \cdot \sin(q_6) + \cos(q_1) \cdot \cos(q_6) \cdot c_{q_{234}} \\ 0 & 0 & 0 \\ I_2 \cdot s(q_{234}) + I_1 \cdot \cos(q_6) \cdot s(q_{234}) - I_3 \cdot \sin(q_2 + q_3) \\ -I_2 \cdot c(q_{234}) \cdot \sin(q_1) + I_1 \cdot \cos(q_6) \cdot \cos(q_1) - I_3 \cdot \sin(q_1) \cdot \sin(q_2 + q_3) - I_5 \cdot \sin(q_1) + I_6 \\ -I_2 \cdot c(q_{234}) \cdot \cos(q_1) - I_1 \cdot \cos(q_6) \cdot \sin(q_1) - I_3 \cdot \cos(q_1) \cdot \cos(q_2 + q_3) - I_5 \cdot \cos(q_1) + I_6 \\ 1 \end{bmatrix} \quad (2.1)$$

Where:  $c(q_{234}) = \cos(q_2 + q_3 + q_4)$  and  $s(q_{234}) = \sin(q_2 + q_3 + q_4)$

Convert coordinate joint operational details is done by solving the direct kinematics problem and coordinate joint operational coordinate conversion is done by solving the inverse kinematics problem.

Inverse kinematics problem allows the calculation [2], [6], [3] coordinates of the joints, which provide end-effector in the desired position and orientation, given the absolute coordinates (operational). When the problem is the inverse kinematics solution, it is the inverse geometrical model. If we cannot find an analytical solution for inverse kinematics problem (which happens quite frequently) we resort to numerical methods, but whose weakness is the sheer volume of calculations. The most common method is Newton-Raphson method. Among these features is remarkable for the way it offers and Khalil Pieper and Paul's method. Pieper and Khalil's method allows solving inverse kinematics problem regardless of the values of the robot geometrical

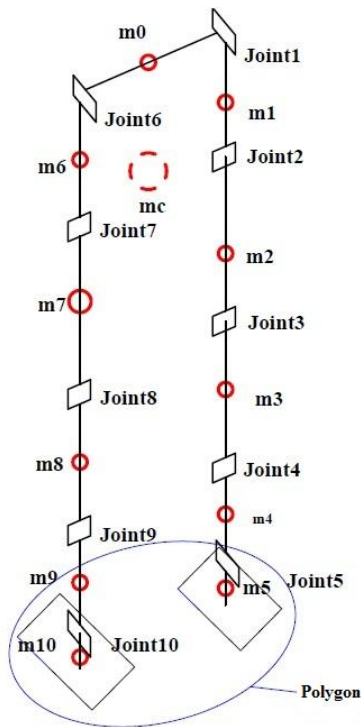
### 3. Centre of gravity

During walking, the feet are subjected to the action of forces [2], [1], [3], [7] and moments of inertia and gravity forces. Balancing the forces of gravity is to reduce the mechanical work consumed for drive motor. The position of equilibrium of a system subject to stationary and links under the action of forces is given, is called stable equilibrium, if for a sufficiently small arbitrary variation of the coordinates of its points and arbitrary speeds sufficiently small print of these points, the system will move all the time remaining in the vicinity of equilibrium position. To determine the center of gravity G of a facility plan is sufficient to determine the position vector  $r_g$  thereof with the relationship:

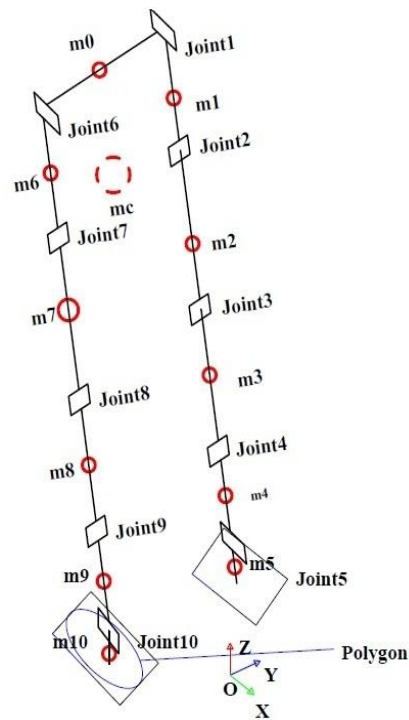
$$\vec{r}_g = \frac{\sum_{i=0}^{10} m_i \cdot r_i}{\sum_{i=0}^{10} m_i} \quad (3.1)$$

$$\vec{r}_g = x_g \cdot \vec{i} + y_g \cdot \vec{j} + z_g \cdot \vec{k} \quad (3,2)$$

Where:  $m_i$  is the mass of the  $i$  element;  $r_i$  is the position vector of center of gravity of element  $i$ .



**Figure 2. Robot model and polygon by two leg ( mc- weight center)**



**Figure 3. Robot model and polygon by one leg**

During walking robot must be stable. This means that its centre of gravity must fall within the polygon (Figure 2.) which consists of the two legs of the robot. If the left leg is raised then the centre of gravity must fall within the polygon of the right leg (Figure 3.). If the projection centre of gravity doesn't fall within the polygon, the robot is unstable. Then it is necessary to tilt (Figure 3.) robot to the right. We know direct and inverse kinematics of the robot and in this way we can calculate the coordinates of the joints. After calculating the joint coordinates it must be checked if the centre of gravity falls within the polygon or, if other compensation is needed for the robot to tilt to the right until the centre of gravity projection falls within the polygon. Easier to solve the problem can be done with an algorithm based on direct and inverse kinematics, with which to verify and ensure the necessary compensation to realise that the position of gravity centre projection of the robot is falling inside the stability polygon.

Bipedal walking is difficult when viewed as a general dynamic system. The dynamics are high degree-of-freedom, nonlinear, under-actuated, naturally unstable, and discretely change from step to step. These combined characteristics place bipedal walking [5] control outside the realm of traditional book control techniques. It is in part due to these difficulties that a large number of different control methods have been developed, and no single method has proven advantageous over the others.

During walking, the feet are subjected to the action of forces [2], [1], [3], [7] and moments of inertia and gravity forces. Balancing the forces of gravity is to reduce the mechanical work consumed for drive motor. The position of equilibrium (Figure 4.) of a system subject to stationary and links under the action of forces is given, is called stable equilibrium, if for a sufficiently small arbitrary variation of the coordinates of its points and arbitrary speeds sufficiently small print of these points, the system will move all the time remaining in the vicinity of equilibrium position.

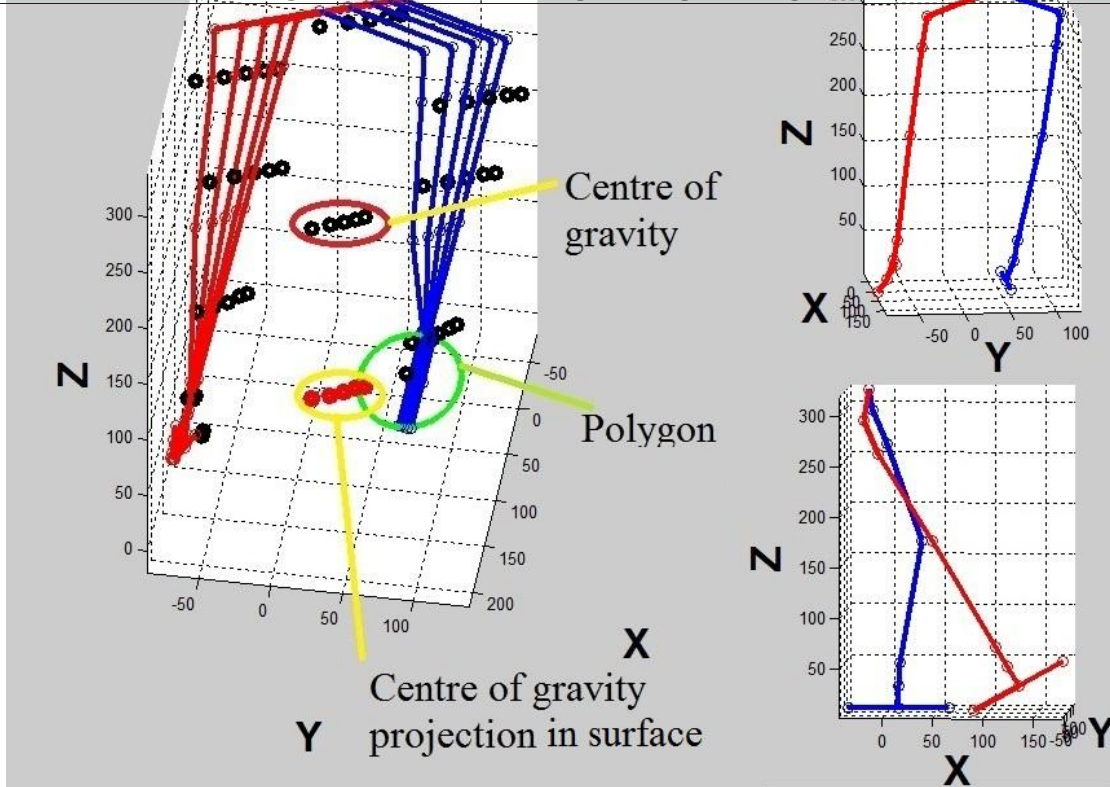


Figure 4. Centre of aravitv simulation one position

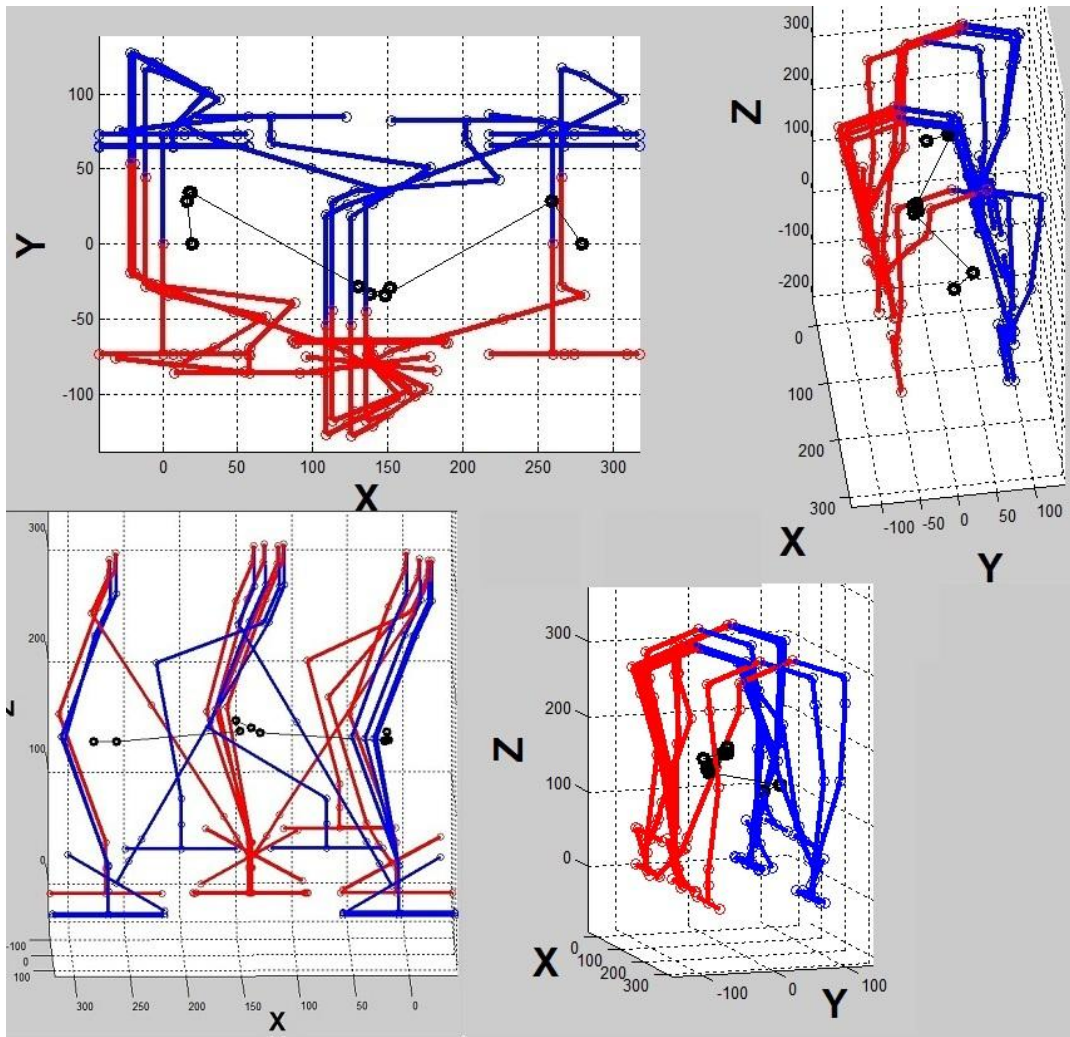


Figure 5. 3D Steping and Center of gravity position



This means that its centre of gravity must fall within the polygon (Figure 4.) which consists of the two legs of the robot. We know direct and inverse kinematics of the robot and in this way we can calculate the coordinates of the joints.

The step (Figure.4.) to raised the left leg or right leg and remains below the leg centre of gravity must fall within the polygon of the remains below the leg. If the projection centre of gravity doesn't fall within the polygon, the robot is unstable. In a Figure 4. is a five-step motion control of the Humanoid robot until a stable position. The only engines give last joints position so you avoid the potential for rollover. In advance placed in the raised leg as as position as a foot heel is in the ground presently hip moving in advance. The Figure 5. may see in 3D step simulation, that the Inverse kinematics solution controlled in path and a direct kinematics is controlled a center of gravity and stability control. So dynamic motion control of the robot is standing in to leg keep up without having to disrupt

#### **4. Conclusio**

If a biped robot's inverse kinematics problem is solved well, then this helps a lot on the stability, because the well positioned ligament's overall centre of weight has to fall in the given sole's polygon, so that the robot wouldn't tumble over. Inverse kinematics problem allows the calculation coordinates of the joints, which provide end- effector in the desired position and orientation, given the absolute coordinates (operational). Easier to solve the problem can be done with an algorithm based on direct and inverse kinematics, with which to verify and ensure the necessary compensation to realise that the position of gravity centre projection of the robot is falling inside the stability polygon.

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